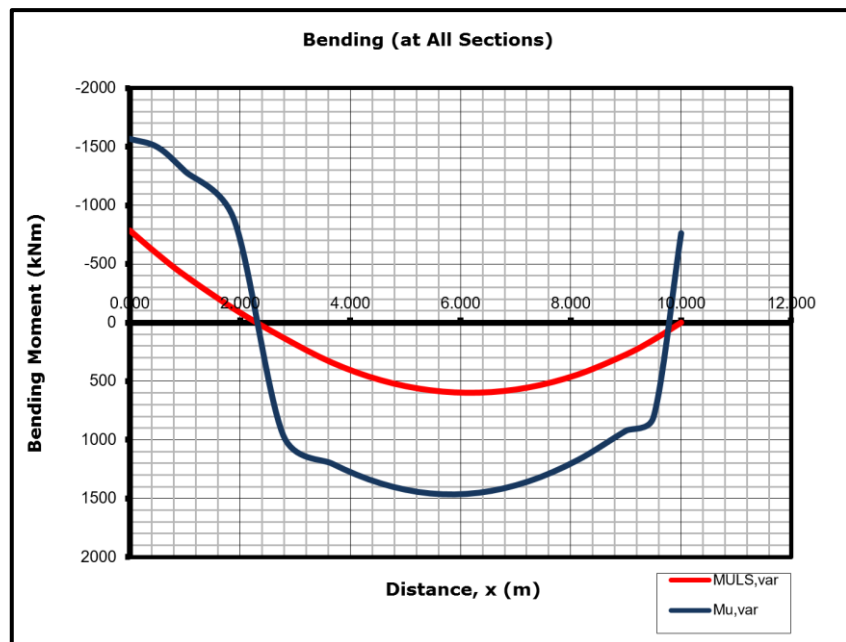


# Prestressed Concrete SLS and ULS External and Equivalent Load Concepts

ITEM	CONTENT																																	
1.0	<p><b>SLS / ULS External Load</b></p> <table border="1" data-bbox="222 314 1062 433"> <tr> <td>Span, L</td> <td>10.000 m</td> </tr> <tr> <td>SLS beam loading, <math>w_{SLS,E/E}</math></td> <td>50.0 kN/m</td> </tr> <tr> <td>ULS beam loading, <math>w_{ULS,E/E}</math></td> <td>70.0 kN/m</td> </tr> </table> <p>Note.</p>	Span, L	10.000 m	SLS beam loading, $w_{SLS,E/E}$	50.0 kN/m	ULS beam loading, $w_{ULS,E/E}$	70.0 kN/m																											
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2.0	<p><b>SLS Equivalent Load</b></p> <table border="1" data-bbox="222 557 1062 759"> <tr> <td>Span, L</td> <td colspan="3">10.000 m</td> </tr> <tr> <td></td> <td><b>L-Sup</b></td> <td><b>Span</b></td> <td><b>R-Sup</b></td> </tr> <tr> <td>Distance between points of inflexion, s</td> <td>2.000</td> <td>8.000</td> <td>2.000 m</td> </tr> <tr> <td>Total drape between points of inflexion, <math>e_d</math></td> <td>56</td> <td>195</td> <td>37 mm</td> </tr> <tr> <td>SLS equivalent load, <math>w_{SLS,E/L} = \pm [8]2]KP_0 \cdot e_d / s^2</math></td> <td>231.6</td> <td>-50.0</td> <td>151.8 kN/m</td> </tr> <tr> <td colspan="4">Note that the equivalent load calculation includes the support peak tendon reverse curvature;</td> </tr> <tr> <td>Dimensions, <math>\{p_1, L-p_1-p_2, p_2\}</math></td> <td>1.000</td> <td>8.000</td> <td>1.000 m</td> </tr> <tr> <td><math>\Sigma</math> SLS equivalent load, <math>\Sigma \{p_1, L-p_1-p_2, p_2\} \cdot w_{SLS,E/L}</math></td> <td>232</td> <td>-400</td> <td>152 kN</td> </tr> </table> <div data-bbox="1083 510 1923 807"> <p><b>Physical Tendon Profile</b></p> </div>	Span, L	10.000 m				<b>L-Sup</b>	<b>Span</b>	<b>R-Sup</b>	Distance between points of inflexion, s	2.000	8.000	2.000 m	Total drape between points of inflexion, $e_d$	56	195	37 mm	SLS equivalent load, $w_{SLS,E/L} = \pm [8]2]KP_0 \cdot e_d / s^2$	231.6	-50.0	151.8 kN/m	Note that the equivalent load calculation includes the support peak tendon reverse curvature;				Dimensions, $\{p_1, L-p_1-p_2, p_2\}$	1.000	8.000	1.000 m	$\Sigma$ SLS equivalent load, $\Sigma \{p_1, L-p_1-p_2, p_2\} \cdot w_{SLS,E/L}$	232	-400	152 kN	
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<p>The SLS equivalent load is chosen to balance the SLS external load by 100%. Note that the total SLS equivalent load will always be zero (cl.A.1.1.1 TR.43). A non-zero value here is an indication that the tendons are not horizontal at termination and thus produces a vertical SLS equivalent load component to a total of this magnitude.</p>																																		
3.0	<p><b>SLS / ULS External Load Effects</b></p> <div data-bbox="235 914 1041 1222"> <p><b>SLS / ULS Bending Moment Diagram (External Effects)</b></p> </div> <div data-bbox="1100 914 1906 1222"> <p><b>SLS / ULS Shear Force Diagram (External Effects)</b></p> </div>																																	
<p>The SLS / ULS external load produce: -</p> <ul style="list-style-type: none"> <li>• SLS / ULS external effects bending moment</li> <li>• SLS / ULS external effects shear force</li> <li>• SLS / ULS external effects reactions.</li> </ul>																																		
4.0	<p><b>(SLS / ULS) Equivalent Load Effects</b></p> <div data-bbox="235 1389 1041 1697"> <p><b>(SLS / ULS) Bending Moment Diagram (Equivalent Load, Primary and Secondary Effects)</b></p> </div> <div data-bbox="1100 1389 1906 1697"> <p><b>(SLS / ULS) Shear Force Diagram (Equivalent Load, Primary and Secondary Effects)</b></p> </div>																																	
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5.0	<p><b>Summation of SLS External Load and (SLS / ULS) Equivalent Load Effects</b></p> <div data-bbox="235 1863 1041 2172"> <p><b>SLS Bending Moment Diagram (External and Equivalent Load Effects)</b></p> </div> <div data-bbox="1100 1863 1906 2172"> <p><b>SLS Shear Force Diagram (External and Equivalent Load Effects)</b></p> </div>																																	
<p>The summation of the SLS external load and the (SLS / ULS) equivalent load <b>effects</b> is <b>effectively zero</b> as the SLS equivalent load was chosen to balance the SLS external load by 100%. Any <b>residual non-zero</b> effect must be resisted by the concrete material itself, this check being undertaken by the SLS stress check or the Magnel Diagram check.</p>																																		
6.0	<p><b>Summation of ULS External Load and (SLS / ULS) Equivalent Load Effects</b></p> <div data-bbox="235 2309 1041 2617"> <p><b>ULS Bending Moment Diagram (External and Equivalent Load Effects)</b></p> </div> <div data-bbox="1100 2309 1906 2617"> <p><b>ULS Shear Force Diagram (External and Equivalent Load Effects)</b></p> </div>																																	
<p>The summation of the ULS external load and the (SLS / ULS) equivalent load <b>effects</b> is <b>not zero</b> as the SLS equivalent load was chosen to balance the SLS external load by 100% and not the ULS external load. This <b>non-zero</b> effect must be resisted by steel reinforcement or the concrete material itself, this check being undertaken by the ULS bending and shear design.</p>																																		

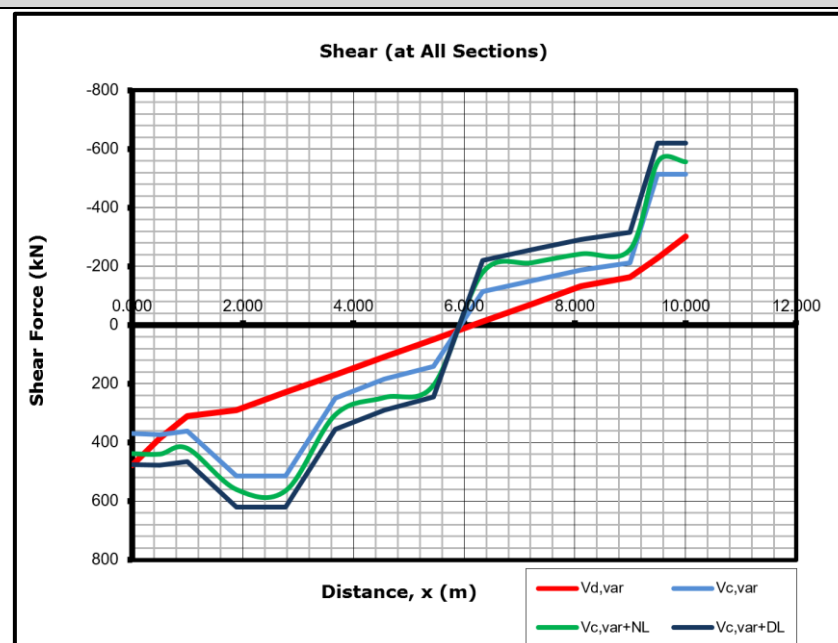
# Prestressed Concrete SLS and ULS External and Equivalent Load Concepts

## 7.0 ULS Bending And Shear Design



$$M_u = f_{pb} A_{ps} (d_{cen} - 0.45x) \text{ [Rectangular] or [Flanged - NA in Flange]}$$

$$M_u = f_{pb} (A_{ps} - A_{pf}) (d_{cen} - 0.45x) + 0.45 f_{cu} (b - b_w) h_f (d_{cen} - 0.45h_f) \text{ [Flanged - NA in Web]}$$



$$V_c = \{V_{co} \text{ uncracked, MIN } (V_{co}, V_{cr}) \text{ cracked}\}$$

$$V_{co} + KP_0 \sin \beta \text{ where } V_{co} = 0.67 b_v h \sqrt{f_t^2 + 0.8 f_{cp} f_t}$$

$$V_{cr} = (1 - 0.55 \frac{f_{pe}}{f_{pu}}) v_c b_v d + M_0 \frac{V}{M}$$

The bending moment capacity,  $M_u$  must be greater than the ULS external effects bending moment plus the (SLS / ULS) secondary effects bending moment,  $M_{ULS} = M_{ULS,E/E} + M_{ULS,S/E}$ . The shear force capacity,  $V_c$  must be greater than the ULS external effects shear force plus the (SLS / ULS) secondary effects shear force,  $V_{ULS} = V_{ULS,E/E} + V_{ULS,S/E}$ . Equivalent loads will automatically generate primary and secondary effects when applied to the structure. SLS calculations do not require any separation of the primary and secondary effects, and analysis using the equivalent loads is straightforward. However, at ULS the two effects must be separated because the secondary effects are treated as applied loads. The primary prestressing effects are taken into account by including the tendon force in the calculation of the ultimate section capacity. This primary prestressing effect is represented by: -

- $f_{pb} A_{ps} (d_{cen} - 0.45x)$  in the bending moment capacity
- $KP_0 \sin \beta$  in the uncracked shear capacity
- $M_0 V/M$  in the cracked shear capacity.